

6.5 Find an Equation for a Line Given the Slope and a Point

Principles of Mathematics 9, pages 330–337

A

1. Find the equation of a line with the given slope and passing through the given point.

a) $m = 2$, $P(4, 5)$

b) $m = -4$, $P(-3, -2)$

c) $m = \frac{3}{5}$, $P(5, -1)$

d) $m = -\frac{1}{4}$, $P(2, 6)$

2. Find the equation of a line with the given slope and passing through the given point.

a) $m = 0$, $P(5, -4)$

b) $m = 3$, $P\left(\frac{2}{3}, \frac{1}{4}\right)$

c) $m = \frac{2}{3}$, $P(0, 0)$

d) $m = \frac{1}{2}$, $P(-3, -4)$

3. Find the equation of a line

a) with a slope of 5, passing through $(2, 3)$

b) with a slope of -4 , passing through $(-3, 5)$

c) parallel to $y = 2x + 5$, passing through $(3, 2)$

d) perpendicular to $y = 3x - 4$, passing through $(5, -3)$

e) parallel to $y = 4$, passing through $(2, 3)$

f) perpendicular to $y = -2$, passing through $(-3, 1)$

4. Find the equation of a line.

a) parallel to $y = \frac{1}{2}x + 3$, passing through the origin

b) perpendicular to $y = -\frac{5}{2}x + 3$, passing through $(-2, -3)$

c) parallel to $y = -2x + 3$, passing through $(0, 0)$

d) perpendicular to $y = 3x + 4$, passing through $(0, 0)$

B

5. Find an equation for the line parallel to $3x + 5y - 4 = 0$, with the same x -intercept as $2x - 3y - 6 = 0$.

6. Find an equation for the line perpendicular to $2x + 5y - 3 = 0$, with the same y -intercept as $2x + 3y + 6 = 0$.

7. In Ottawa, you can ride on a tour bus for a fixed price plus a variable amount that depends on the length of the trip. The variable cost is \$2/km and a 20-km trip costs \$55.

a) Determine the equation relating cost, C , in dollars, and distance, d , in kilometres.

b) Use your equation to find the cost of a 15-km tour.

c) Graph the relation.

d) Use the graph to find the cost of a 15-km tour.

8. Refer to question 7.

- a) Copy and complete the table to solve the problem using a third method. Explain this method.

Distance (km)	Cost (\$)	First Differences
2	19	
3	21	2
4		
5		
6		

- b) Use all three methods (equation, graph, and table) to determine how far you could travel on the tour bus for \$105.
- c) Use each method to determine the cost of a 10.5 km tour.
- d) Describe at least one advantage and one disadvantage to each method of solution.
9. **Use Technology** A city taxi charges \$3/km and a fixed cost. A 5-km taxi ride costs \$21. Use *The Geometer's Sketchpad*[®] to find
- a) the fixed cost
- b) the equation relating cost, C , in dollars, and distance, d , in kilometres
- c) the equation using another method to check your results.

C

10. Ahmed has been running at an average speed of 15 km/h towards the finish line of a 45 km race for 2 h, when he sees a checkpoint sign shown.

Finish Line 15 km

- a) What does the ordered pair (2, 15) mean?
- b) The slope is $m = -15$. What does this value represent? Why is it negative?
- c) Determine the value of b .
- d) Write an equation relating distance and time.
- e) Graph the relation. What is the meaning of the d -intercept?
- f) How long will the race take, in total?
- g) Has Ahmed reached the halfway point of his race yet? Explain.
11. Emeline has been driving at an average speed of 100 km/h towards Hamilton for 2 h, when she sees the sign shown.

Hamilton 300 km

- a) What does the ordered pair (2, 300) mean?
- b) The slope is $m = -100$. What does this value represent? Why is it negative?
- c) Determine the value of b .
- d) Write an equation relating distance and time.
- e) Graph the relation. What is the meaning of the d -intercept?
- f) How long will the car drive take, in total?
- g) Has Emeline reached the halfway point of her trip yet? Explain.